# Expert RF Feature Extraction to Win the Army RCO Al Signal Classification Challenge

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Abstract—Automatic modulation classification is a challenging problem with multiple applications including cognitive radio and signals intelligence. Most of the existing efforts to solve this problem are only applicable when the signal to noise ratio (SNR) is high and/or long observations of the signal are available. Recent work has focused on applying shallow and deep machine learning (ML) to this problem. Feature generation, where raw signal information is transformed prior to attempting classification is a key part of this process. A big question that researchers face is whether to let the deep learning system infer the relevant features or build expert features based on expected signal characteristics. In this paper, we present novel signal feature extraction methods for use in signal classification via ML. The deep learning and combined approaches are discussed in a simultaneous publication. Expert features were utilized via ensemble leaning and shallow neural networks to win the Army Rapid Capability Office (RCO) 2018 Signal Classification Challenge. The features include both standard statistical measurements such as variance and kurtosis, as well as measurements tailored for specific waveform families. We discuss the best statistical descriptors along with a ranked list of signal features and discuss individual feature importance. We then demonstrate our implementation of these features and discuss effectiveness in estimating different modulation classes. The methods discussed when combined with deep learning are capable of correctly classifying waveforms at -10 dB SNR with over 63% accuracy and signals at +10 dB SNR with over 95% accuracy from an Army RCO provided training set.

**Index Terms**—modulation, feature extraction, neural networks, machine learning, decision trees, wireless communication, signals intelligence, feature importance

# Introduction

All conventional communications systems are designed with the assumption that the transmitter and receiver are cooperative and have full knowledge of the waveform being exchanged. However, there are scenarios where the receiver does not know what waveform (i.e. modulation, coding, etc.) has been transmitted. Classical examples include cognitive radio network (i.e. a new terminal enters a network and needs to figure out what waveform is being used), and signals intelligence (i.e. interception of adversary's communications). The problem of waveform classifications, or more narrowly, modulation recognition has been studied for decades [ModRec]. Given the implication of SIGINT<sup>1</sup> applications before cognitive radio, much of the work had not been

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published. Key early work is done by Azzouz & Nandi [Nandi1], [Nandi2], [Azz1], [Azz2].

The fundamental approach taken by most authors has been to find data reduction functions that accentuate the differences between different waveforms. These functions are applied to input samples and decision is made by comparing the values against a set of multi-dimensional thresholds. Determining the threshold values by hand becomes impractical as the number of clusters and/or functions grows. The idea to apply neural networks to help make these decisions has been around for decades [Azz2]. However, it is only recently that our understanding of machine learning combined with enormous increase in computational resources has enabled us to use ML techniques with many data reduction functions against many simultaneous waveforms.

# **Challenge Description**

The Army Rapid Capability Office is seeking innovative approaches to leverage artificial intelligence (AI) to conduct blind radio frequency signal analysis. To this end, they published a labeled modulation classification dataset and created a competition [Army] to properly classify a pair of unlabeled test sets. This paper details the efforts of The Aerospace Corporation's Team Platypus to build a modulation classification system via *traditional* expert features and shallow machine learning classifiers. In this context, shallow refers to the fact that the ML classifier will not build features out of the raw data, instead the classifier will only use the expert features provided. The winning submission from Team Platypus utilized a combination of this expert feature engineering with a deep neural network trained on raw IQ<sup>2</sup> samples, which are described in a simultaneous companion publication.

The training dataset [Mitre] consists of 4.32 million signals each of which containing 1024 complex (IQ) points and a label indicating the modulation type and SNR. Modulation type is selected from one of 24 digital and analog modulations (including a noise class), with AWGN at six different signal-to-noise ratios (-10, -6, -2, +2, +6, or +10 dB). The complete dataset included 30,000 rows for each modulation and SNR configuration. Sample rate is selected from a set (200, 500, 1000, or 2000 ksps), and symbol rate is selected from a set (4, 8, 16, or 32 samples per symbol). Neither of the rate parameters is included in the label.

- 1. Signals Intelligence
- 2. In-Phase & Quadrature

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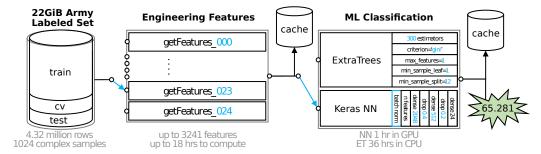


Fig. 1: Data flow through engineering features evaluation to classification and scoring. Light-blue denote the many variable parameters available. In the Army dataset, cv is short for cross validation.

The competition consisted of assigning a likelihood score to each of the 24 possible modulation classes for each of the 100,000 rows in a pair of unlabeled test sets.

Classifier performance is evaluated via a pre-defined equation based on the well-known log loss metric, sometimes referred to as cross-entropy loss. The traditional cross validation log loss equation is:

$$logloss = -\frac{1}{N} \sum_{i=1}^{N} \sum_{j=1}^{M} y_{ij} \log p_{ij}$$
 (1)

Where N is the number of instances in the test set, M is the number of modulation class labels (24),  $y_{ij}$  is 1 if test instance i belongs to class j and 0 otherwise,  $p_{ij}$  is the predicted probability that observation i belongs in class j. Per [Mitre] this is then scaled between 0 and 100.

$$score = \frac{100}{1 + logloss} \tag{2}$$

Note:

- A uniform probability estimate would yield a score of 23 935 not zero.
- To get a perfect 100 score participants would need to be both 100% correct and 100% confident of every estimation.

We will also use a more standard  $F_1$  metric for each modulation is used. This is an excellent measurement of classifier performance since it uses both recall r and precision p, which better account for true positives and false positives:

$$r = \frac{\sum true\ positive}{\sum false\ negative + \sum true\ positive}$$
 (3)

$$p = \frac{\sum true \ positive}{\sum false \ positive + \sum true \ positive}$$
(4)

$$F_1 = \frac{2}{\frac{1}{r} + \frac{1}{p}} \tag{5}$$

#### **Approach**

Team Platypus' approach to solve this modulation classification problem is to combine deep neural networks and a shallow learning classifiers leveraging custom engineering features. Both of these are supervised machine learning systems. The engineering features that we applied to this data set are based on traditional signal processing and digital communication techniques. Some shallow learning classifiers, such as Extremely Randomized Trees (ERT) [ModRec] and Random Forests [Nandi1], are decision-tree ensemble methods designed to be robust to overfitting. Ensemble

methods train multiple classifiers that will ultimately decide the class using a majority vote or similar metric. These constituent classifiers learn to be different by using different training datasets and/or random parameters independent of the output. The majority voting over this diverse set tends to mitigate the possible overfitting of the constituent classifiers. This is a highly desirable property that becomes even more useful in applications where the test data may have some deviations compared to the labeled train data. The other advantage of decision-tree ensemble methods is that they provide an estimate on whether the features are useful in the classification process. This is further described in Feature Importance Evaluation.

Figure 1 shows the general flow of data through the engineering features evaluation system. The labeled training data is split into training, cross-validation, and testing using a 70%-15%-15% split. When using neural networks, the cross-validation set is the only fair method to prevent network overfitting. When using ERT, the 15% allocated to cross-validation is appended to the training set. Using the Army RCO score metric, the final version of this system scored 65.281. This equates to a cross-validation log loss of 0.532. The output of each step is written to large cache files to enable quick evaluation of new features and integration into the next processing pipeline.

Not pictured are the later steps that merge these expert features with the ResNeXt convolutional deep neural network and a temperature calibration step; all of which yielded an internal final score of 76.422, which equates to a final cross-validation log loss of 0.308.

## **Measurement Vectors**

Multiple transformations of the raw complex measurement vectors were made as intermediate steps to feature extraction. Most of the reduction functions (i.e. feature extraction) are applied to each of the transformed vectors. The following sections describe these methods.

#### I. Brute-Force PSK & QAM Symbol Estimation

Many common modulations can be expressed in the following form:

$$z_{(t)} = \sum_{n=0}^{\infty} x_{[n]} \cdot h_{(t-T_0 - nT_s)}$$
(6)

Where  $z_{(t)}$  is the received baseband continuous-time signal,  $x_{[n]}$  are the complex-valued data symbols (each selected from some fixed constellation, depending on modulation),  $T_0$  is the time offset of the first symbol,  $T_S$  is the symbol period, and  $h_{(t)}$  is the pulse-shaping impulse response. This broad description includes all

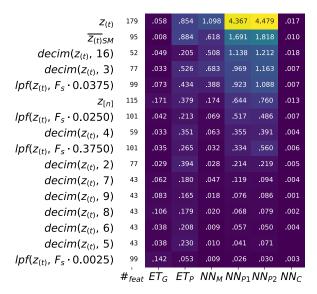


Fig. 2: Ranked importance of measurement vectors. Numbers in the heat map indicate residual crossvalidation logloss. See Feature Importance Evaluation for a description of the ranking statistics.

ordinary PSK<sup>3</sup>, APSK<sup>4</sup>, and QAM<sup>5</sup> modulations, and it can be extended to include variants such as OQPSK<sup>6</sup>,  $\frac{\pi}{4}$  QPSK, etc.

Given  $z_{(t)}$  (or its discrete-time approximation), the blind symbol recovery operation determines  $T_0$ ,  $T_S$ , and  $h_{(t)}$  in order to estimate  $x_{[n]}$  without attempting to determine the precise modulation type.

For the Army RCO Challenge, this process is greatly simplified because  $T_S$  may only take one of four discrete values: 4, 8, 16, or 32 samples per symbol. Similarly,  $h_{(t)}$  is always the simple rectangular pulse or a root-raised-cosine (SRRC) filter with one of a few rolloff parameters. We simply attempt recovery for all possible combinations of these parameters, estimate SNR using the  $M_2M_4$  method [Pauluzzi], and keep the configuration with the highest SNR. (Note the generic, constant-envelope  $M_2M_4$  method will return biased results for APSK and QAM modulations, but the max-SNR point is still accurate enough for timing estimation.) The pulse-shaping library can be simplified by pre-calculating discrete filter responses for  $T_S = 4$ , and decimating all other inputs to match that effective sampling rate.

One notable special case is OQPSK. Since the dataset has neither phase nor frequency offsets, this signal can be trivially "converted" to QPSK by delaying the real-part of the input signal by  $\frac{T_S}{2}$ . This method would not work for real-world signals, but is adequate for the Challenge.

The only remaining parameter is  $T_0$ , which we estimated using one of two methods. The first is Seung Joon Lee's "absolute value nonlinearity" method [Lee]. The second is simple brute-force search with a step size of 1/16th of the symbol period, retaining the output with the highest SNR (as above). The former method is selected because it ran considerably faster and returned essentially identical results.

Given all input parameters, we decimate  $z_{(t)}$  to four samples per symbol, optionally delay the in-phase part of the signal (see

- 3. Phase Shift Keying
- 4. Amplitude and Phase Shift Keying
- 5. Quadrature Amplitude Modulation
- 6. Offset Quadrature Phase Shift Keying

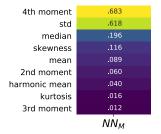


Fig. 3: Ranked importance of descriptive statistics. See Feature Importance Evaluation for a description of the  $NN_M$  statistic.

above), apply the selected matched filter, then finally estimate  $x_{[n]}$  by applying piecewise quadratic interpolation to the filtered signal.

The resulting symbol set is not used directly, but is used to calculate various statistics (such as the decision-directed noise power) that are used as machine-learning features.

### II. Phase Histogram

The purpose of this metric is to estimate how many different modulated phases were present in each waveform. The goal is to provide a way to differentiate between different M-ary PSK waveforms.

To this end, we first calculate the instantaneous phase of each input signal  $\angle z_{(t)}$ . Then divide the interval from 0 to  $2\pi$  into 32 equal-size bins and count the number of samples within each bin. The resulting histogram is circular-shifted such that the largest count is in first bin. The output feature set is simply the vector of 32 counts, one per bin. Since the input vector size is fixed at 1024 samples, no further normalization is required.

# **Descriptive Statistics**

Descriptive statistics were applied to all vector measurands and accounted for 37% of all engineering features in the most expansive feature functions. Figure 3 details which were of most importance. Note that some of these features are nonlinear combinations of each other.

# **Custom Features**

#### I. Decision-Directed Noise Estimation

Decision-directed noise estimation operates on recovered symbols. Given a fixed constellation, the estimated noise for each symbol x[n] is simply the difference vector to the nearest constellation point. This nearest-neighbor calculation can be run quickly using k-d trees. The estimated noise power for each constellation is simply the mean-square power of these difference vectors.

Normally, this process would require gain and phase estimation, to correctly align the received signal with the reference constellation. For the Challenge, all input signals had a fixed gain and no phase or frequency offset, so this step is not required.

The estimated noise is calculated separately for a constellation from each of the following modulation types: BPSK<sup>7</sup>, QPSK<sup>8</sup>, 8PSK<sup>9</sup>, 16PSK, 16APSK, 32APSK, 16QAM<sup>10</sup>, 32QAM, and 64QAM. Each such estimate is then used as a machine-learning feature.

- 7. Binary Phase Shift Keying, each symbol representing 1 bit
- 8. Quadrature Phase Shift Keying, each symbol representing 2 bits
- 9. 8, 16, and 32 value PSK represent 3, 4, and 5 bits per symbol
- 10. Similar to PSK Modulations, 16, 32, and 64 QAM represent 4, 5, and 6 bits per symbol

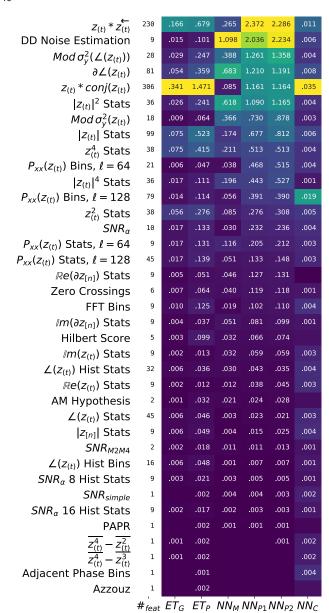


Fig. 4: Ranked importance of individual features.  $NN_{P1}$  differs from  $NN_{P2}$  in that these permutaiton importances were derived from two separately trained neural networks.  $\#_{feat}$  denotes total number of features in each category noted left.  $P_{xx}$  denotes power spectral density. Notice that the color map is normalized per column since metrics are difficult to compare otherwise.

#### II. Hilbert Score

An analytic signal is a complex-valued function that has no negative frequency components. The real and imaginary parts of an analytic signal are real-valued functions related to each other by the Hilbert transform. The negative frequency components of the Fourier transform of a real-valued function are superfluous, due to the Hermitian symmetry of such a spectrum. Many techniques for modulating and demodulating single-sideband waveforms use a Hilbert transformer as a core block.

One the most challenging waveforms we had to deal with in this challenge is differentiating between the AM-SSB<sup>11</sup> and AM-DSB<sup>12</sup> pair, especially given the modulation bandwith was as little as 0.5% of the total bandwidth in some cases. The initial intent of this method is to convert time domain data to

analytic domain. Another modulation pair that our classifiers had issues with is differentiating QPSK and  $\frac{\pi}{4}$  QPSK waveforms. The "Hilbert score" feature is developed to help our classifier reduce confusion among these similar modulations.

The metric is defined as follows:

$$HSM = |\sum H\left(real\left(z[t] \cdot z_0\right)\right)] + \sum H\left(imag\left(z[t] \cdot z_0\right)\right)| \quad (7)$$

Where HSM is the Hilbert score metric, H(z) is the Hilbert transform, z is the vector of input samples, and  $z_0$  is a rotation phasor at either 0 or 45°. This figure of merit proved to be useful to our shallow classification algorithm.

#### III. DC Power

This metric is simply the 0th bin of the FFT of the complex input vector. The feature consists of the real and imaginary part of this value, considered separately.

### IV. Simple SNR Estimation

In principle, given that at the time this metric is implemented we were already using more precise SNR estimators, the usefulness of this simpler and noisier estimator may not have been justified. However, the extremely randomized tree classifier reported this metric as initially useful and we will use it as a baseline for other metrics.

$$SNR_{simple} = \frac{\frac{1}{2N}\sum|z[t]|^2}{Var(|z|)}$$
 (8)

#### V. $M_2M_4$ SNR Estimation

Pauluzzi in [Pauluzzi] presents a comparison of different SNR estimators for phase-shift keyed (PSK) channels with additive white Gaussian noise (AWGN) noise. Though many of those methods are of limited accuracy at very low SNR, the  $M_2M_4$  method still performs well under such conditions.

 $M_2M_4$  method uses the second and fourth moments of a waveform to estimate its SNR. Though it is only directly applicable to constant-envelope signals, it is still useful for relative comparisons under almost any conditions. For simplicity, we use the generalized complex form (m-ary PSK) regardless of modulation:

$$SNR_{M_2M_4} = \frac{\sqrt{2M_2^2 - M_y}}{M_2 - \sqrt{2M_2^2 - M_4}} \tag{9}$$

#### VI. $\alpha$ SNR Estimation

Many digital communication algorithms require knowledge of the operating signal-to-noise ratio (SNR). Different algorithms exist that estimate signal and noise power or the actual ratio between these two. However, most of the known techniques at low SNR either fail or have very large variance. In order to estimate SNR below 5 dB, we developed a technique that builds on the work by Davenport [Davenport]. This approach to SNR estimation introduces a non-linear technique that uses the inherent properties of non-linear devices, such as a limiter or an automatic-gain-control (AGC) device, to estimate negative SNRs. In our case, the non-linear function used is a sign function. The properties of these devices used for SNR estimation are well known and have been carefully studied in the literature [Davenport]. Similarly to many tracking loops operating at low SNRs, this method multiplies the

- 11. Single Sideband Amplitude Modulation
- 12. Dual Sideband Amplitude Modulation

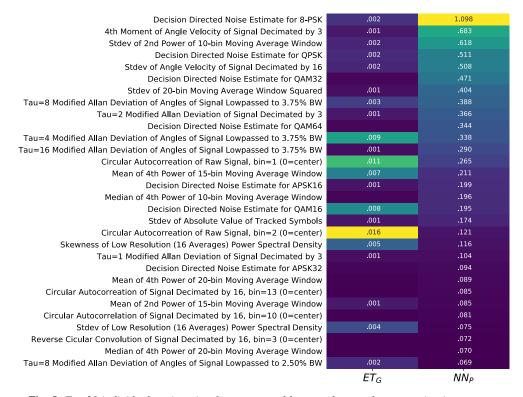


Fig. 5: Top 30 individual engineering features sorted by neural network permutation importance.

current sample of a given waveform by the sign of the previous sample (under an assumption of multiple samples per symbol).

$$S_{re}[k] = sign(z_{re}[t] \cdot z_{re}[t-1]))$$

$$S_{im}[k] = sign(z_{im}[t] \cdot z_{im}[t-1]))$$

$$\alpha = \frac{1}{N} \sum sign(S_{re}[t] + S_{im}[t])$$

If the signal is modulated, this process will introduce an error every time the sign of a symbol changes. If the signal has no modulation present, then this block is simply equivalent to a magnitude block. This operation is performed independently on the real and imaginary component of the signal. The metric can be plugged into the result from [Davenport] where for a non-coherent receiver, the SNR can be approximated by:

$$SNR_{\alpha} = \frac{\alpha^2}{1 - \alpha^2} \tag{10}$$

A comparison of the Simple,  $M_2M_4$ , and  $\alpha$  SNR estimators are shown in Figure 6 and Figure 7.

#### VII. N-M-D Power Estimation

In the  $SNR_{M_2M_4}$  method, we see that the differences of signal moments can be part of the core of SNR estimation algorithms. As we explored generating new features to aid our shallow classifier, we introduced a new feature that would simply compute the difference of two moments  $M_x - M_y$ . This proved to be of extremely useful as a feature generating function. This function is not meant to compute an approximation metric for estimating SNR but as an intermediate feature in the signal classification process.

#### VIII. AM Hypothesis Testing

The sample AM signals all were baseband analytic signals with a residual carrier close to zero frequency. The feature we

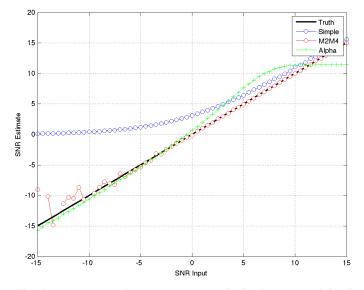


Fig. 6: Comparison of SNR estimation methods of a PSK modulated signal including novel  $SNR_{\alpha}$  metric.

designed to distinguish double sideband (DSB) vs. single sideband (SSB) depends on this assumption.

First, the carrier frequency and phase is estimated with the three-sample discrete-Fourier-spectrum interpolator described in section III.D. of Macleod [Macleod]. Multiplication by the inverse of the estimated carrier signal (with unit amplitude) makes the estimated carrier DC. Next, two transformations of the resulting analytic signal are compared.

- 1. The mean is simply subtracted from the signal: if the signal is DSB, this would result in its coherent demodulation.
  - 2. Non-coherent demodulation is achieved by taking the mod-

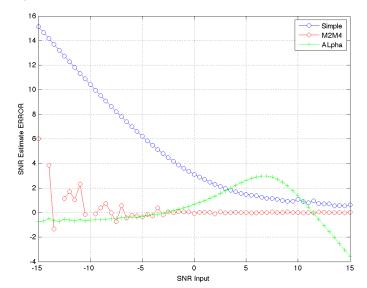


Fig. 7: Error of SNR estimation methods.

ulus of the analytic signal and subtracting off its mean over the sample time.

The feature used is the energy of the difference between these two transformations, divided by the energy of the first transformation. When close to zero, the signal would likely be DSB and, when close to one, SSB.

# Modified Allan Deviation $(Mod\sigma_v^2(\tau))$

Typically used as a tool to characterize the stability of time & frequency sources, we applied the modified Allan deviation [NIST] statistic to a number of angle measurements taken of the raw signal and several low-pass transformations. These were computed with a Butterworth 5th-order low pass with cutoff frequencies at 2.5% and 37.5% of the max & min sample rates in order to filter for narrowband modulations.

$$\angle z(t) = arctan2(real(z(t)), imag(z(t)))$$
 (11)

This effectively captured the variability of phase over a number of averaging taus including 1, 2, 4, 8, 16, and 32 complex samples. A nice implementation can be found in the AllanTools<sup>13</sup> python module.

# X. Zero Crossings

Some modulations such as  $\frac{\pi}{4}$  QPSK are designed such that transitions between symbols avoid passing through the origin. In general, this is used to reduce peak-to-average signal power ratios, which removes certain design constraints on signal amplifiers.

The zero-crossing metric is selected to detect these types of modulations. Considering the real and imaginary parts separately, the metric examines the sign of each sample and counts the total number of transitions from positive to negative or vice versa.

The zero-crossing feature is calculated on the z(t) directly, but is most valuable on the multiple lowpass transformations.

# **Feature Importance Evaluation**

When single or multiple features were added to the feature extraction engine they are computed over all signals in the training

set. These features were then appended to the shared cache of features from prior runs. This new larger feature set is then sent to classification and a score is produced.

Initial feature importance is derived from the delta change in score from run to run. This method requires close tracking of every feature and is ambiguous when multiple features or vectors of features are added simultaneously. To address this, several more precise approaches are used to evaluate performance.

A comparison of the following feature importance statistics can be found in Figures 2, 3, 4, and 5.

# Gini Importance ( $ET_G$ )

Gini importance or mean decrease in impurity, is implemented in sklearn for Random Forest type classifiers as the feature\_importances\_ attribute. After training this metric is available with no additional effort or computation, giving immediate feedback. This metric is useful for the Extra Trees classifier specifically, but is only available for ensemble-type classifiers. While his metric is computationally free, there are several pitfalls described by [Cutler] such as incorrect valuation of correlated or random features that make Gini importance of limited use.

# Permutation Importance (ET<sub>P</sub> & NN<sub>P</sub>)

Permutation importance [Parr] can be computed for any classifier by creating a logloss benchmark score for a test set (Eq 1), then randomly permuting 1 feature across all signals. This has the effect of keeping the population statistics of that feature constant, but removing it's contribution to the overall logloss score. Permutation importance is then calculated by subtracting the predicted logloss score of the permuted set from the prior benchmark. Since the shape of the input data is preserved, a trained classifier does not need retraining and is therefor a fast metric. We denote permutation importance for ExtraTress and our shallow neural network as ET<sub>P</sub> & NN<sub>P</sub> respectively. Permutation importance provides the fastest & most robust method for evaluating feature importance for any classifier.

## Drop-Column Importance $(NN_C)$

Drop-column importance [Parr] provides perhaps the highest quality estimate of individual feature importance, but is extremely computationally expensive and may take weeks or months to compute for even moderately sized neural networks. An initial logloss benchmark is computed, then a feature is dropped across the entire test population, requiring retraining of the classifier for every feature. Resulting importance residuals are difficult to judge since the scale is so small and correlated features often yield near zero change when removed.

## Max-Column Importance $(NN_M)$

Max-column importance is a metric used in Figure 2, 3, and 4, to denote the maximum  $NN_P$  across many features grouped into a set. This is computed since the quantiles of importances are heavily skewed toward zero since there are so many (1269) features being compared.

#### Recursive Feature Elimination

Recursive Feature Elimination (RFE) is a technique originally designed for gene selection [Guyon]. This method evaluates the a feature importance estimate of choice after training, then prunes a number of features each step attempting to build a sorted list. This is implemented within sklearn.feature\_selection as RFE. This is

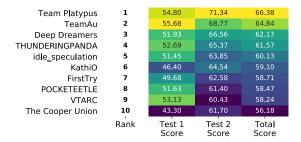


Fig. 8: Final Army RCO AI Signal Classification leaderboard.

also *highly* computationally intensive since it requires retraining the classifier every step. There is value in RFE for comparing total number of features to logloss score, especially when building a classifier for low SWAP<sup>14</sup> implementations where computation is limited.

# **Classification Strategy & Scores**

From the beginning of the challenge it was clear that in scenarios where cross validation labeled sets were used to evaluate the performance of classifiers, that ERT have worse overall performance than neural networks. However, given that the nature of the unlabeled sets was unknown, both techniques were pursued.

There were two unlabeled sets released to competitors. Estimates generated for the first set using our deep neural network estimator resulted in very low and inconsistent scores. It was apparent that the data was very unlike the training data initially provided. Team Platypus estimates that only half of the first unlabeled set was like the training set. Only the ERT classifier was applied to that set due to its resiliency to overfitting. Only one of the competitors achieved a higher score (0.8 points) for this set.

The challenge administrators disclosed that the second set contained data 95% like the training set. As such, a combination of a ResNeXt deep convolutional network combined with a shallow two-layer neural network comprised of engineering features was used to submit the winning prediction. Team Platypus held the highest submission score for the duration of the challenge.

#### Performance

The accuracy of estimation can be visualized as a confusion matrix, shown in Figure 12. Each row represents the true waveform, while each column is the estimated probability. The diagonal values correspond to the 'correct' estimate. Brighter colors indicate higher confidence (e.g. the top left square indicates almost 100% correct identification of the BPSK modulation). This view allows us to quickly identify waveforms that are challenging for our classifier such as the narrowband CPFSK/FSK/FM.

The  $F_1$  score (see Challenge Description) provides another view of the same data. Note that while BPSK is correctly identified 100% of the time, it is not always identified with 100% precision, making the  $F_1$  score less than 1.0. The performance of the classifier decreases at lower SNR. For example, at 10 dB the  $F_1$  score is perfect for most of the waveforms (Figure 10). The overall classifier accuracy versus SNR is shown in Figure 9. Note that we achieve about 50% accuracy even at -10 dB SNR, which is significantly better than previously published results.

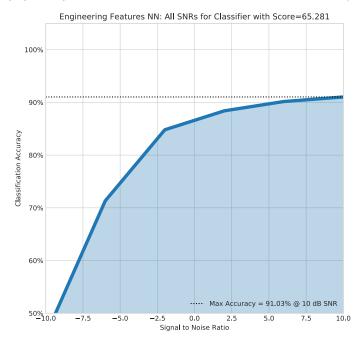


Fig. 9: Classifier Accuracy vs SNR.

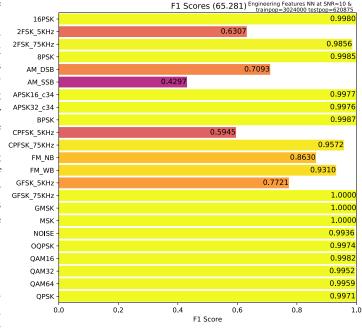


Fig. 10:  $F_1$  scores at 10 dB SNR signals only.

## Conclusion

The robust results presented in this paper show the significant progress that has been made in application of machine learning over the past decade. However, it is important to note that the test cases offered by the Challenge are somewhat unrealistic. Realworld scenarios would include non-idealities like those found in [OShea].

In regard to feature importance there were a number of interesting results. We emphasize that while Gini importance  $(ET_G)$  can approximate neural network permutation importance  $(NN_P)$ , it can be very misleading when given duplicate or random features. Drop-column importance provides a metric that gives an absolute value of the individual contribution of a feature, but is

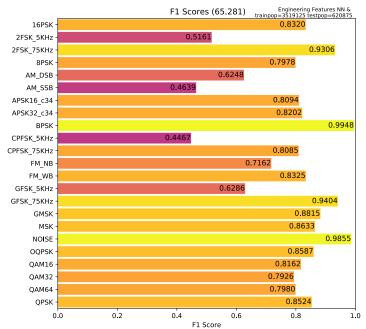


Fig. 11:  $F_1$  scores for all test data.

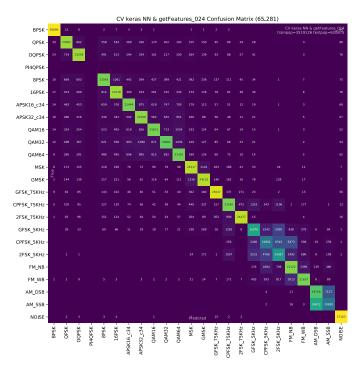


Fig. 12: Confusion matrix for all test data.

prohibitively computationally expensive and with correlated features provides almost no value. We generally found permutation importance from our neural networks to be the best measure of feature value in our classifiers, though all methods still generally suffer when features correlate with other features.

We suggest that further research utilize the best statistics and features described herein to achieve modulation classification estimates robust to the traditional pitfalls of deep neural networks, which include generated adversarial networks like those found in [Dong] and [Moosavi] as well as overfitting due to lack of truth data.

# Acknowledgements

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# REFERENCES

[Army] ARMY RCO AI Signal Classification Challenge. (2018). Retrieved from https://www.challenge.gov/challenge/army-signal-classification-challenge/

[Mitre] MITRE Challenge. (2018). Retrieved from https://sites.mitre.org/ armychallenge/

[Guyon] Guyon, I., Weston, J., Barnhill, S., & Vapnik, V., "Gene selection for cancer classification using support vector machines", Mach. Learn., 46(1-3), 389-422, 2002. doi:10.1023/A:1012487302797.

[Pauluzzi] Pauluzzi, D. & Beaulieu, N., "A comparison of SNR estimation techniques for the AWGN channel," IEEE Trans. on Comm., vol. 48, no. 10, pp. 1681–1691, Oct. 2000. doi:10.1109/26.871393.

[Davenport] Davenport, W., "Signal-to-noise ratios in band-pass limiters," J. Appl. Phys., vol. 24, no. 6, pp. 720–727, June 1953. doi:10.1063/1.1721365.

[Springett] Springett, J., & Simon, M., "An analysis of the phase coherent-incoherent output of the bandpass limiter," IEEE Trans. on Comm. Technology, vol. 19, no. 1, pp. 42–49, Feb. 1971. doi:10.1109/tcom.1971.1090611.

[Lee] Lee, Seung Joon. "A new non-data-aided feedforward symbol timing estimator using two samples per symbol." IEEE Communications Letters 6.5 (2002): 205-207. doi:10.1109/4234.1001665.

[Geurts] Geurts, P., Ernst, D. & Wehenkel, L. Mach Learn (2006) 63: 3. doi:10.1007/s10994-006-6226-1.

[NIST] NIST SP 1065: Handbook of Frequency Stability Analysis. 2008. doi:10.6028/nist.sp.1065.

[ModRec] Aisbett, Janet. "Automatic modulation recognition using time domain parameters." Signal Processing 13.3 (1987): 323-328. doi:10.1016/0165-1684(87)90130-7.

[Nandi1] Nandi, Asoke K., and Elsayed Elsayed Azzouz. "Algorithms for automatic modulation recognition of communication signals." IEEE Transactions on communications 46.4 (1998): 431-436. doi:10.1109/26.664294.

[Nandi2] Nandi, A. K., and Elsayed Elsayed Azzouz. "Automatic analogue modulation recognition." Signal processing 46.2 (1995): 211-222. doi:10.1016/0165-1684(95)00083-p.

[Azz1] Azzouz, Elsayed, and Asoke Kumar Nandi. Automatic modulation recognition of communication signals. Springer Science & Business Media, 2013. doi:10.1007/978-1-4757-2469-1.

[Azz2] Azzouz, Elsayed Elsayed, and Asoke Kumar Nandi. "Modulation recognition using artificial neural networks." Automatic Modulation Recognition of Communication Signals. Springer, Boston, MA, 1996. 132-176. doi:10.1007/978-1-4757-2469-1 5.

[Macleod] Macleod, M.D. "Fast Nearly ML Estimation of the Parameters of Real or Complex Single Tones or Resolved Multiple Tones." IEEE Transactions on Signal Processing 46, no. 1 (1998): 141–148. doi:10.1109/78.651200.

[Cutler] Cutler, A., & Breiman, L. (2018). Random Forests. Retrieved from https://www.stat.berkeley.edu/~breiman/RandomForests/cc\_home.httm#varimp

[Parr] Parr, T., Turgutlu, K., Csiszar, C., & Howard, J. (2018, March 26). Beware Default Random Forest Importances. Retrieved from https://explained.ai/rf-importance/

[OShea] T. J. O'Shea, T. Roy and T. C. Clancy, "Over-the-Air Deep Learning Based Radio Signal Classification," in IEEE Journal of Selected Topics in Signal Processing, vol. 12, no. 1, pp. 168-179, Feb. 2018. doi:10.1109/JSTSP.2018.2797022.

[Dong] Dong, Yinpeng, Fangzhou Liao, Tianyu Pang, Hang Su, Jun Zhu, Xiaolin Hu, and Jianguo Li. "Boosting Adversarial Attacks with Momentum." 2018 IEEE/CVF Conference on Computer Vision and Pattern Recognition (June 2018). doi:10.1109/cvpr.2018.00957.

[Moosavi] Moosavi-Dezfooli, Seyed-Mohsen, Alhussein Fawzi, and Pascal Frossard. "DeepFool: A Simple and Accurate Method to Fool Deep Neural Networks." 2016 IEEE Conference on Computer Vision and Pattern Recognition (CVPR) (June 2016). doi:10.1109/cvpr.2016.282.